Faculty of Engineering Electrical Engineering Department Second Year

Numerical Analysis
Interpolation and
Polynomial Approximation
Sheet \# 2

## Solve for best fit with calculation of coefficient of determination the following problems:

## Prob. \#1

The values of $\sin x$ are given below for different values of $x$. Find the value of $\sin 42^{\circ}$.

| x | $40^{\circ}$ | $45^{\circ}$ | $50^{\circ}$ | $55^{\circ}$ | $60^{\circ}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{y}=\sin \mathrm{x}$ | 0.64279 | 0.70711 | 0.76604 | 0.81915 | 0.86603 |

Prob. \#2

From the following table estimate the number of students who obtained marks in the examination between 50 and 55.

| Marks | $35-45$ | $45-55$ | $55-65$ | $65-75$ | $75-85$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| No. of students | 31 | 42 | 51 | 35 | 31 |

Prob. \#3
Using Newton's forward interpolation formula find the value of $\sin 52^{\circ}$ from the following data. Estimate the error.

| $x$ | $40^{\circ}$ | $45^{\circ}$ | $50^{\circ}$ | $55^{\circ}$ | $60^{\circ}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $y=\sin x$ | 0.64279 | 0.70711 | 0.76604 | 0.81915 | 0.86603 |

Prob. \#4
Using Newton's divided difference interpolation, find $y(10)$ given that

$$
y(5)=12, y(6)=13, y(9)=14, y(11)=16
$$

Prob. \#5
Find $f(8)$ by Newton's divided difference formula, for the data

| $x$ | 4 | 5 | 7 | 10 | 11 | 13 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $f(x)$ | 48 | 100 | 294 | 900 | 1210 | 2028 |

(A.U Apr/May 2005)

Prob. \#6
The Newton forward divided-difference formula is used to approximate $f(0.3)$ given the following data.

| $x$ | 0.0 | 0.2 | 0.4 | 0.6 |
| :---: | ---: | ---: | ---: | ---: |
| $f(x)$ | 15.0 | 21.0 | 30.0 | 51.0 |

Prob. \#7

Use Stirling's interpolation formula to find $y_{3.25}$ from the following data:

| $x$ | 2 | 2.5 | 3.0 | 3.5 | 4.0 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $y=f(x)$ | 49225 | 48316 | 47236 | 45926 | 44306 |

Prob. \#8
Using Newton's backward formula, find the polynomial of degree 3 passing through $(3,6)$, $(4,24),(5,60)$ and $(6,120)$.

Prob. \#9
Find $\mathrm{y}(35)$, by using the given table
x $20 \quad 30 \quad 40 \quad 50$
y 512439346243

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